

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS General Certificate of Education Ordinary Level

STATISTICS Paper 2	Octo	4040/22 ober/November 2013
CENTRE NUMBER	CANDIDATE NUMBER	
CANDIDATE NAME		

Candidates answer on the question paper.

Additional Materials: Pair of compasses

Protractor

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** questions in Section A and not more than **four** questions from Section B.

If working is needed for any question it must be shown below that question.

The use of an electronic calculator is expected in this paper.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

This document consists of 20 printed pages.



2 hours 15 minutes

Section A [36 marks]

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Answer all of the questions 1 to 6.

1	Eve	ents A	A, <i>B</i> , <i>C</i>	and D are four	of the possibl	e outcomes	of an e	experiment such that	
				P(A) = 0.15,	P(B) = 0.2,	P(C) = 0.4	and	P(D) = 0.24.	
	(i)	If ev	ents A	and <i>B</i> are inde	ependent, find				
		(a)	P(<i>A</i> ∩	n <i>B</i>),					
									[2]
		(b)	P(<i>A</i> ∪	J <i>B</i>).					
									[2]
	(ii)	If ev	ents C	and <i>D</i> are mut	ually exclusiv	e, find			[-]
		(a)	P(<i>C</i> ∩	n <i>D</i>),					
									[1]
		(b)	P(<i>C</i> \	J D).					

.....[1]

(i)	The annual salaries of the employees at a company have a mean of $\$m$ and a standard deviation of $\$s$, where $s \ne 0$. A new employee arrives at the company and is paid an annual salary of $\$m$. The mean and standard deviation of the salaries of the employees are now recalculated to include the salary of the new employee.
	For each of the mean and the standard deviation, state whether it will increase, decrease, or stay the same when this new employee's salary is included.
	Mean
	Standard deviation[2]
(ii)	At another company, at the end of 2011, the employees' annual salaries had a mean of \$12000 and a standard deviation of \$1000. During 2012, each of the employees' salaries increased by 5%. At the end of that year they each also received an annual bonus of \$200.
	Calculate the mean and standard deviation of the annual incomes (salaries plus bonuses) of the employees at the end of 2012.
	Mean \$
	Standard deviation \$[4]

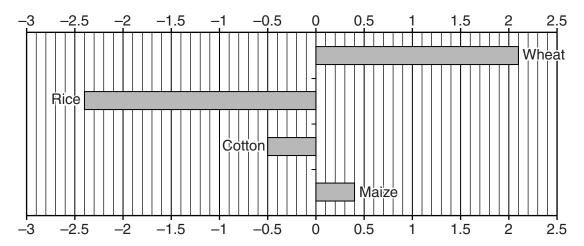
2

		4
3	The	ana and Bella are playing a game. y each have 4 cards, which are numbered 1, 2, 3 and 4. h shuffles her own cards and turns one over at random.
	(i)	If the cards show the same number, Ariana wins and Bella must pay Ariana \$3. If the cards show different numbers, Bella wins and Ariana must pay Bella \$1.
		By finding the probabilities of Ariana and Bella winning, show whether or not the game is fair.
		[3]
	(ii)	In a second game the numbers shown on the cards are added together. If the total is 4 or less, Ariana wins and Bella must pay Ariana \$5. If the total is 5 or more, Bella wins.
		If the game is to be fair, how much should Ariana pay Bella if Bella wins?
		\$[3]

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4	The pupils in a class should arrive for registration at 9.00 am. On one particular day, 25 pupils were early, with a mean arrival time of 8.51 am. On the same day, 9 pupils were late with a mean arrival time of 9.21 am, and 2 pupils arrived at 9.00 am exactly.
	If x represents the number of minutes a pupil was late (a pupil who was early would have a negative value of x),
	(i) find Σx , and hence find the mean arrival time for all 36 pupils.
	$\sum x = \dots$
	Mean =[3]
	If $\sum x^2 = 5096$ for the 36 pupils,
	(ii) find the standard deviation of x, correct to one decimal place.
	[3]

5 The change in a country's annual production (in millions of tonnes) of 4 commodities between 2011 and 2012 is shown in the change chart below.

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Change in annual production between 2011 and 2012 (in millions of tonnes)

The quantity produced (in millions of tonnes) of the 4 commodities in 2011 in this country is shown in the table below.

Commodity	Quantity produced in 2011 (millions of tonnes)	Quantity produced in 2012 (millions of tonnes)
Wheat	78.6	
Rice	99.2	
Cotton	22.6	
Maize	17.3	

(i) Use these data and the change chart to find the quantities of the commodities produced in 2012 and complete the table. [2]

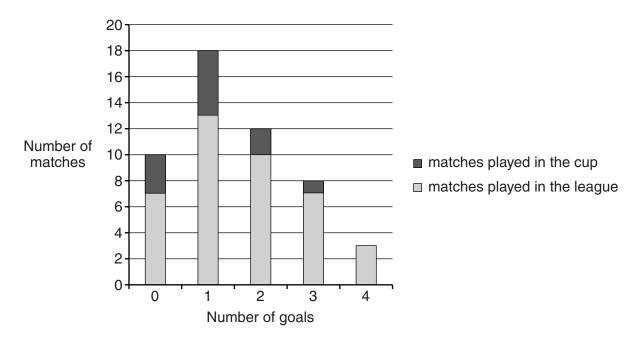
				[3]
ata ana adva	antage of a dual h	oar chart over a cha	nge chart	

6 (a) For each of the following state whether the variable is discrete or continuous and whether it is qualitative or quantitative.

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		Discrete or Continuous	Qualitative or Quantitative	
(i)	the heights of the players in a football competition			[1]
(ii)	the towns of birth of the players in a football competition			[1]

(b) A football team used the diagram below to illustrate the number of goals it had scored per match in a season in both the league and cup competitions.



(i) State the full name given to this type of diagram.

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(ii) Explain why the above diagram is more appropriate than a histogram to illustrate these data.

(iii) Find the proportion of matches played in the cup in which the team scored 2 or more goals.

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Section B [64 marks]

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Answer not more than **four** of the questions 7 to 11.

Each question in this section carries 16 marks.

(a) The total number of visitors at a tourist attraction has been recorded for every quarter over a three-year period.	
(i) Explain why it might be appropriate to calculate moving average values wher establishing the trend in the number of visitors.	
[1]	
(ii) If an <i>n</i> -point moving average is to be calculated, state an appropriate value for <i>n</i> .	(
[1]	`
(iii) State, with a reason, whether centring would be necessary in this case.	(i
[2]	

(b) A hospital records the number of patients admitted at two-monthly intervals over a period of two years and the results are shown in the table below, together with the 6-point moving average values for these data.

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		Number of patients	6-point total	6-point moving average value	Centred moving average value
	Jan – Feb	241			
	Mar – Apr	208			
	May – Jun	<i>x</i> =			
2010			1272	212	
	Jul – Aug	185			
			1290	215	
	Sep – Oct	209			
			1290	215	
	Nov – Dec	261			
			1296	216	
	Jan – Feb	259			
			<i>y</i> =	Z=	
	Mar – Apr	208			
			1323	220.5	
	May – Jun	174			
2011			1332	222	
	Jul – Aug	197			
	Sep – Oct	224			
	Nov – Dec	270			

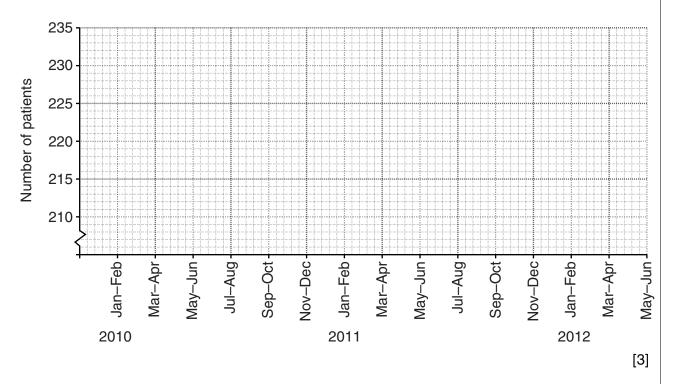
(i) Calculate the values of x, y and z and insert them in the table.

(ii) Calculate the centred moving average values and insert them in the appropriate places in the table.

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[3]

(iii) Plot the centred moving average values on the grid below and draw a trend line through the points.



(iv) Explain what the trend line you have drawn tells you.

 [1]

The seasonal component for Mar - Apr is -11.25.

(v) Estimate the number of patients admitted to the hospital during the period Mar – Apr 2012.

8 The students at a college take one of three programmes of study: Physics, Chemistry and Mathematics (PCM) or Physics, Chemistry and Biology (PCB) or Economics, Geography and Mathematics (EGM). The numbers of students who study each programme are shown in the table below.

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	PCM	PCB	EGM	TOTAL
Male	60	40	40	140
Female	40	90	30	160
TOTAL	100	130	70	300

	TOTAL	100	130	70	300	
Find the pro	bability that	a student cl	nosen at rar	ndom		
(a) is a ma	ale studying F	PCM,				
						r.1
(b) is fame	do.				•••••	[1]
(b) is fema	ue,					
						[1]
(c) is stud	ying Physics	as part of th	neir program	nme,		
						[1]
(d) is stud	ying PCB, giv	ven that they	/ are male.			
						[1]
	ent students rogramme of		at random,	find the pro	obability tha	t they are taking
						[3]

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(i)

(ii)

			andom, find the	e probability th	at they are each	For Examiner's Use
					থে	
•	•		n subject that th	ney study: one t	extbook for each	
		a student taki	ng each progr	amme of study	y must buy, and	
	Course	PCM	PCB	EGM		
	Number of textbooks				[1]	
		ned by a stud	ent at the coll	ege is lost at r		
(a) belongs	to a student or	n the PCM pro	gramme,			
					[3]	
(b) is a Mat	hematics textb	ook.			[0]	
					[2]	
)	dents are requested. Physics, Chemic Geography. Find how macomplete the probability the probability the complete the com	dents are required to buy text Physics, Chemistry and Biolo Geography. Find how many textbooks complete the table below. Course Number of textbooks If one of the textbooks own probability that it (a) belongs to a student or	dents are required to buy textbooks for each Physics, Chemistry and Biology and two te Geography. Find how many textbooks a student taki complete the table below. Course PCM Number of textbooks If one of the textbooks owned by a stud probability that it	clents are required to buy textbooks for each subject that the Physics, Chemistry and Biology and two textbooks for each geography. Find how many textbooks a student taking each programplete the table below. Course	dents are required to buy textbooks for each subject that they study: one to Physics, Chemistry and Biology and two textbooks for each of Mathema Geography. Find how many textbooks a student taking each programme of study complete the table below. Course PCM PCB EGM Number of textbooks	dents are required to buy textbooks for each subject that they study: one textbook for each shysics, Chemistry and Biology and two textbooks for each of Mathematics, Economics Geography. Find how many textbooks a student taking each programme of study must buy, and complete the table below. Course

9 (a) The values of a variable are formed into a grouped frequency distribution, with one of the classes stated as 50 - 60. State the true class limits of this class if the variable is

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	Lower class limit	Upper class limit	
(i) the ages of the residents in a block of flats,			[1]
(ii) the lengths of some rods, measured in mm, to the nearest mm,			[1]
(iii) the lengths of some rods, measured in mm, to the nearest 10 mm.			[1]

(b) A fisherman recorded, in grams (g), to the nearest 100 grams, the masses of 100 fish he had caught in river *A*.

Mass of fish (grams)	Number of fish	Cumulative frequency
100 – 200	12	
300 – 400	31	
500 – 700	29	
800 – 1000	14	
1100 – 1400	8	
1500 – 2000	4	
2100 – 3000	2	

	appropriate measure of central tendency to use in this case.	
		[2]
(ii)	Find the cumulative frequencies and complete the table above.	[1]
(iii)	Without drawing a graph, calculate an estimate of the interquartile range masses of the fish.	of the

(i) State, with a reason, which of the mean or the median would be the more

.....[6]

(iv)	The fisherman also recorded the masses of 100 fish caught in river <i>B</i> and found the interquartile range of the masses of these fish to be 352 g. Explain what this tells you about the masses of the fish caught in river <i>B</i> compared to those caught in river <i>A</i> .	For Examiner's Use
	[1]	
(v)	Without drawing a graph, calculate an estimate of the percentage of fish in river $\it A$ with a mass of less than 650 g.	
	[3]	

			16
10			esser classifies the expenditure on her business into three categories: Rent, int and Wages.
	The	price hou	of Rent has increased from \$240 per month in 2010 to \$256 per month in 2012. e relative of Equipment in 2012 is 110, taking 2010 as base year. rly rate of the Wages of her employees has decreased by 2% between 2010 and
	(i)	(a)	Calculate the price relative, to the nearest whole number, of Rent for 2012, taking 2010 as base year.
		(b)	Explain what the price relative of 110 for Equipment indicates.
			[3]
		(c)	State the price relative of Wages for 2012, taking 2010 as base year.
		(d)	Present the price relatives for 2010 and 2012 for each of Rent, Equipment and Wages in a suitable table.

[2]

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The hairdresser wishes to calculate a weighted aggregate cost index, using weights

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cald	culate	d in 2010, for the three categories.
(ii)	(a)	Briefly describe how these weights could be calculated.
		[1]
		weights in 2010 for Rent, Equipment and Wages were calculated as 7, 2 and 5 ectively.
	(b)	Calculate, to the nearest integer, a weighted aggregate cost index for 2012, taking 2010 as base year.
		[3]
	(c)	Her total expenditure on the hairdressing business in 2010 came to \$5760. Use your answer to part (b) to estimate, to the nearest dollar, her total expenditure on the business in 2012.
		[2]
	(d)	Give two possible reasons why this estimate might be very inaccurate.
		Reason 1
		Reason 2
		[2]

11	A gr cha	mall village has a population of 60 people aged 10 and over. roup of researchers wish to find out what the people of the village think about proposed nges to the timetable for the buses that pass through the village. Each researcher has a of the population and thinks of a different way to select a sample.				
	(i)	and	first researcher plans to stand at the village bus stop at 7 am on a Monday morning ask the first six people from the population who come to wait for a bus. Explain why might not produce a reliable sample.			
			[2]			
	(ii)	A second researcher decides to take a simple random sample of size six from the population of 60 people.				
		(a)	Explain what the researcher would need to do with the population list before being able to select the sample from a random number table.			
			[2]			
		(b)	Use the random number table below, starting at the beginning of the first row and working along the row, to select a simple random sample of size six from the population of 60 people, ensuring that no one is selected more than once.			
			RANDOM NUMBER TABLE			
			15 08 73 00 60 15 31 52 86 47 82 99 04 33			
			23 05 65 27 46 13 81 50 49 34 29 08 94 72			

(iii)	A third researcher decides to take a systematic sample of size six from the population.						
	(a)	Explain clearly how they should use a random number table to select the first value for such a sample.	Examiner's Use				
		[1]					
	(b)	Use the random number table below, starting at the beginning of the first row and working along the row, to select a systematic sample of size six.					
		RANDOM NUMBER TABLE					
		36 04 85 06 63 22 16 64 12 51 25 92 74 43					
		35 75 21 44 56 20 83 59 98 35 27 08 14 69					
		[3]					

[Question 11 continues on the next page]

The table below shows the population, split into three different age groups.

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	10 – 18 years	19 – 65 years	66 years and over	TOTAL
Number of people	20	30	10	60

(iv)	A fourth researcher decides to take a random sample of size six, stratified by age group.									
	(a)	State how many people from each age group would be needed for such a sample.								
		10 – 18 years								
		19 – 65 years								
		66 years and over[1]								
	(b)	Explain clearly what the researcher would need to do before selecting the random sample, stratified by age group, from a random number table.								
		[2]								
	(c)	Use the random number table below, starting at the beginning of the first row and working along the row, to select a random sample of size six, stratified by age group, ensuring that no one is selected more than once. Use every number if the age group to which it relates has not yet been fully sampled.								
	RANDOM NUMBER TABLE									
		17 55 82 25 07 16 35 42 89 37 91 98 24 38								
		77 29 38 02 47 19 80 53 16 40 28 07 94 73								
		[2]								
	(d)	Explain why a random sample, stratified by age group, might be a good idea in this situation.								
		[1]								

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